

## SPECIAL ISSUE PAPER

# A systematic literature review of the use of formal methods in medical software systems

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**Abstract**

The use of formal methods is often recommended to guarantee the provision of necessary services and to assess the correctness of critical properties, such as functional safety, cybersecurity, and reliability, in medical and health care devices. In the past, several formal and rigorous methods have been proposed and consequently applied for trustworthy development of medical software and systems. In this paper, we perform a systematic literature review on the available state of the art in this domain. We collect the relevant literature on the use of formal methods for modeling, design, development, verification, and validation of software-intensive medical systems. We apply standard systematic literature review techniques and run several queries in well-known repositories to obtain information that can be useful for people who are either already working in this field or planning to start. Our study covers both quantitative and qualitative aspects of the subject.

**KEYWORDS**

formal methods, systematic literature review, medical device software

## 1 | INTRODUCTION

In modern medical devices, human safety depends upon the correct operation of software controlling the device: Software malfunctioning can cause injuries to, or even the death of, patients. A crucial issue is how to guarantee that medical software has all the qualities (eg, safety, security, and dependability) expected for critical components. One way to improve and assess software quality, as suggested by literature,<sup>1-3</sup> is to use formal methods or in general rigorous methods for design, validation, and verification of medical software. Some processes for improvement of medical standards, based on formal approaches, have already been proposed,<sup>4-6</sup> although their adoption in industrial applications is rather limited.

The overall aim of this paper is twofold: (1) to provide guidance to researchers starting to work on this topic and (2) to assess the state of the art that is more useful for researchers already working on this subject. We have applied a systematic literature review (SLR) process to the topic of rigorous methods for designing and validation of medical software and systems by following the guidelines presented in literature<sup>7-9</sup> with slight improvements such as a wider range of repositories is queried for information retrieval and the subject is covered from both quantitative and qualitative aspects. Through this analysis, we give an overview of the research literature about formal methods applications to model, to verify, and to validate medical systems. Moreover, we include processes and tools that translate models written using formal languages in machine code. We would like to underline that the SLR carried out in this work considers only formal methods applied to medical device/software. Other processes applied to medical device/software are outside of our goal (eg, code implementation, testing,<sup>8</sup> and hardware configuration).

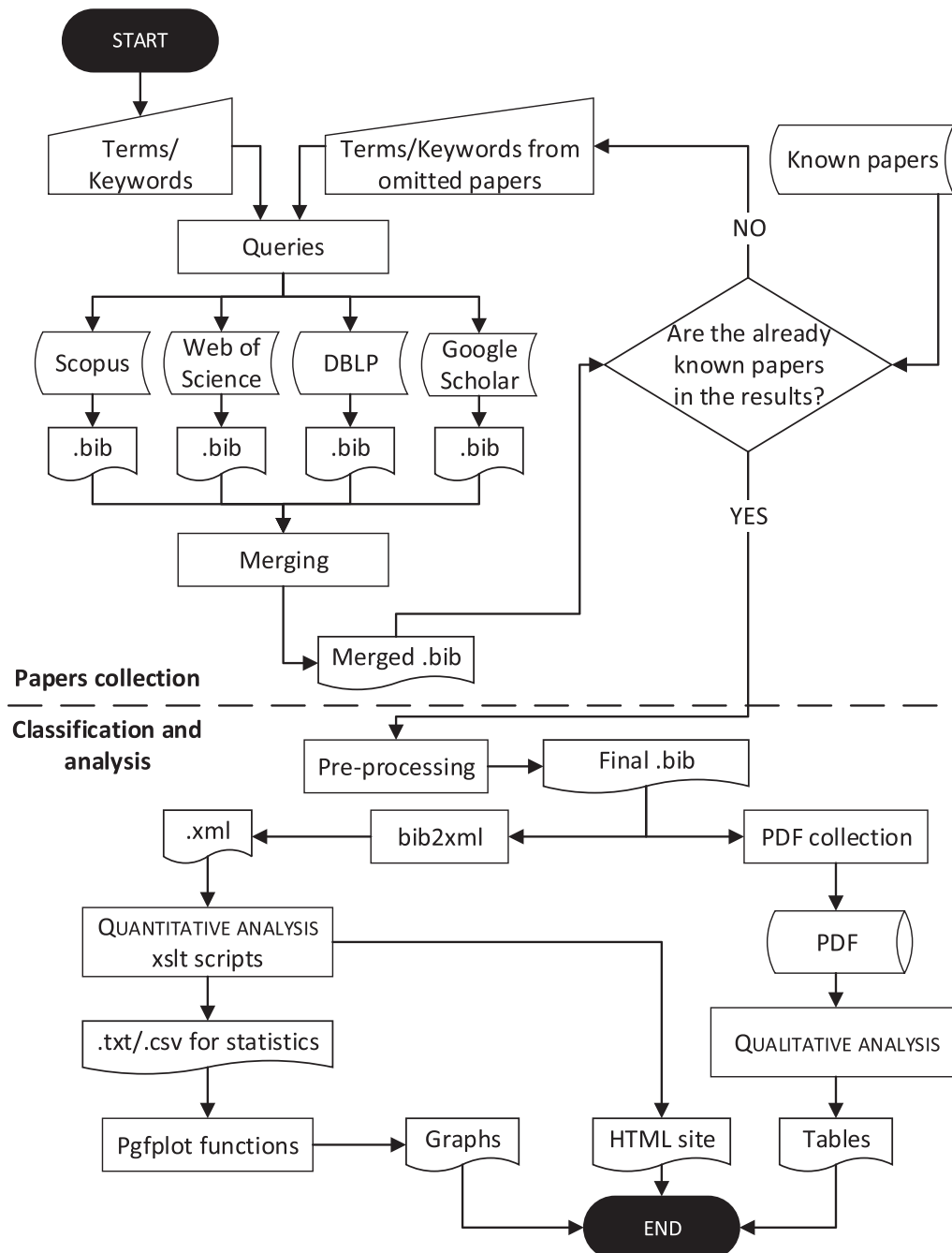
The goals of our SLR are (1) to gather a sufficient number of relevant articles, (2) to perform a series of analyses, and (3) to publish results of findings to allow researchers to browse in the collected data. This activity follows a systematic process to avoid possible biases to include as much information as possible, but at the same time capable of identifying only relevant papers.

This paper extends our previous work<sup>10</sup> in several directions: We consider a larger amount of repositories during the collection of papers, we implement an improved and strengthened filtering process to exclude papers not related to the topic under investigation, and we integrate the quantitative analysis, in addition to a qualitative analysis, in terms of notations used, case studies, and activities performed.

The article is organized as follows: In Section 2, we explain the SLR process we applied to collect and analyze papers. In Section 3, we show the data sources we use. In Section 4, we perform an analysis of data by answering a set of research questions (RQ1-RQ7) to extract useful information. In Section 5, we discuss some limitations of the SLR process. The article is concluded in Section 6.

## 2 | THE SLR PROCESS

An SLR is the review of a clearly formulated question that uses systematic and explicit methods to identify, select, appraise relevant research, collect, and analyze data from the studies that are included in the review.<sup>11</sup> An SLR defines a precise process for literature review: Criteria for inclusion and exclusion are explicitly stated, and therefore, it provides a transparent and repeatable selection process. The final aim is to minimize bias and increase objectivity of the review outcomes.



**FIGURE 1** Systematic literature review process

Figure 1 shows our devised SLR process; it is divided into 2 main steps:

- **Papers collection:** collect papers for the SLR analysis;
- **Classification and analysis:** classify and analyze papers obtained in the first step.

The final goal of this process is to provide a list of papers that fit the topic of the SLR and several analyses over the selected papers. The first step consists in the definition of terms used to perform queries on different databases. Once the user runs queries on databases (see Section 3 for further details on databases), the results can be saved in different file formats. We have chosen the `.bib` file type, which is very often used for the bibliography; it adopts a standardized format, and it is easily processable with tools and own scripts since it is a textual file. After that, all obtained `.bib` files are merged into the `Merged.bib` file. The user checks whether all already known papers (a list of papers already known to the user about the topic) are included into the file `Merged.bib`. If not, he or she has to identify terms from omitted papers and rerun queries to also include them. Despite the fact that the list of known papers is manually selected based on user's previous experience, the chances of introducing a possible bias are minimal. This is because the set of previously known papers is only used for checking the completeness of the query and for the analysis we consider all the papers resulting from the search.

Then the classification and analysis phase starts. First, the preprocessing activity is performed (eg, delete duplicates and unrelated papers). The result of preprocessing is the `Final.bib` file ready for the analysis. Then `Final.bib` is translated into the `.xml` file using our own `bib2xml` script. Starting from the `.xml` file, we perform QUANTITATIVE ANALYSIS (see Section 4.1) to automatically extract a set of statistical information. Quantitative analysis has a low degree of human interaction because only fields in the bibliographic entries are used (eg, year, type of publication, and number of citations). We use our own scripts written using Extensible Stylesheet Language Transformation (`.xslt`), and results are saved into `.txt` or `.csv` files. After that, results are plotted using `pgfplot` package provided by It should be L<sup>A</sup>T<sub>E</sub>X. The quantitative analysis results are statistical data obtained using mathematical measurements and calculations.

Starting from `Final.bib`, we collect PDF files of resulted papers and complete a QUALITATIVE ANALYSIS to provide more technical details (eg, the case study analyzed and the notation used). Qualitative analysis (see Section 4.2) requires user interaction since the content of the papers must be analyzed.

Furthermore, starting from the `.xml` file, we generate a HTML website by using the `.xslt` script. The website contains all publications listed in the `Final.bib` file and is available online.\*

### 3 | PAPERS COLLECTION

During a preliminary analysis,<sup>10</sup> we used only Scopus (<http://www.scopus.com>), but we missed some relevant papers published in journals and in proceedings not included in the Scopus database. For this reason, now we consider other repositories besides Scopus, ie, Web of Science (<https://apps.webofknowledge.com>), DBLP (<http://dblp.uni-trier.de/>), and Google Scholar (<https://scholar.google.com/>). We do not consider IEEE Xplore (<http://ieeexplore.ieee.org/>), Springer (<http://www.springer.com>), and ACM Digital Library (<http://dl.acm.org/>) because they are already included in Scopus and DBLP. Furthermore, we noticed that the search function of IEEE Xplore has some limitations: During the search activity, some queries returned unrelated results, which did not contain the terms entered in the query.

Scopus is the largest database of scientific publications owned by Elsevier; it contains scientific journals, books, and conference proceedings. It encloses more than 60 million records, over 21 500 peer-reviewed journals, over 360 trade publications, 7.2 million conference papers, 27 million patents, and 5000 articles-in-press from international publishers including Cambridge University Press, IEEE, Nature Publishing Group, Springer, ACM Digital Library, and Wiley. It includes more than 113 000 books. Thomson Reuters maintains Web of Science that provides a citation search. It gives access to several databases in different disciplinary researches: Conference Proceedings Citation Index (covers more than 160 000 conference titles), Science Citation Index Expanded (covers more than 8500 journals encompassing 150 disciplines), Social Sciences Citation Index (covers more than 3000 journals in social science), Arts & Humanities Citation Index (covers more than 1700 arts and humanities journals), and Book Citation Index (covers more than 60 000 books). DBLP provides open bibliographic information of major computer science journals and proceedings. It contains more than 3 million publications relating to more than 4500 conferences and more than 1400 journals. This service is provided by University of Trier and Schloss Dagstuhl. Google Scholar furnishes a way to search literature, and it contains a large quantity of documents. It is possible to search across many sources: articles, theses, books, abstracts, court opinions, academic publishers, professional societies, online repositories, universities, and patents.

Given the repositories listed above, we have chosen a set of terms based on the goal of the SLR to perform queries.<sup>†</sup> The queries are a combination of terms using “and” and “or” logical operators. Most queries perform the search only in titles, while few of them are executed on author keywords

\* The list of publications is available at <http://cs.unibg.it/bonfanti/FMMedicalDeviceSLR/>.

† The list of queries is available at <http://cs.unibg.it/bonfanti/FMMedicalDeviceSLR/listquery.html>.

**TABLE 1** Terms used in the queries

Approaches	Application Fields	
Formal	Medical device/s	Syringe pump
Formal method/s	Medical software	ECG
Formal specification/s	Medical system/s	e-Health
Formal modeling/ modeling	Medical pump	Medical communication protocol
Formal validation	Hemodialysis	Stereoacuity test
Formal code generator/ generation	Infusion pump	Pulse oximeter
Formal certification	Pacemaker	Imatinibdose

Abbreviation: ECG, electrocardiography.

and abstracts. This limitation is due to the search functions provided by the repositories, as shown below. Due to the intrinsic limited functionality, the number of queries run for each repository is not the same.

Scopus has the most performing search system. It allows to execute an advanced search, eg, by title (TITLE), by author keywords (AUTHKEY), by abstract (ABS), or by their discrete combination. Furthermore, it allows to search terms that start with a prefix or end with a suffix by using "\*" symbol (eg, "method\*" means "method, methods, methodology, methodologies").

Web of Science is similar to Scopus, but it does not allow to perform an advanced search, eg, by keywords or by author keywords.

DBLP has a limited search technology. It is not possible to specify the search field (eg, title and keywords), and it is not allowed to perform the words search by suffix or prefix.

Google Scholar provides 2 search options: The first limits the search to the title, and the second extends the search anywhere in the documents (title, content, keywords, and authors) at the same time. The latter option introduces many papers out of scope, so only the first one is considered. Furthermore, Google Scholar allows to search for specific authors, specific publication venues, and time intervals. We do not use these types of searches because we do not know in advance the data we should look for.

Regarding the terms and keywords, we have identified 2 subsets of possible terms based on our experience. The 2 subsets of terms are combined in the searches: The first one refers to the use of formal techniques, and the second one refers to the application field; the 2 sets are displayed in Table 1.

We have combined all the terms in the first column with all the terms in the second column. Moreover, while "Formal" was searched only in the title, the others were searched in TITLE, ABS, and AUTHKEY, if the search engine provides this kind of search. For instance, in SCOPUS, we have performed the following queries:

TITLE = (formal) AND TITLE-ABS-AUTHKEY = (infusion pump)

TITLE-ABS-AUTHKEY = (formal validation) AND TITLE-ABS-AUTHKEY = (hemodialysis)

After the execution of queries in the databases, we found 359 papers including duplicates because some papers fit in more than one query, either in the same repository or the other.

By following the process defined in Figure 1, the next step consists of exporting all papers found in the repositories and merging them in the Merged.bib file.

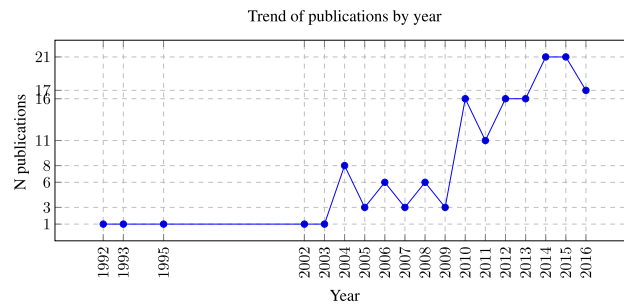
## 4 | CLASSIFICATION AND ANALYSIS

Before performing classification, we make preprocessing activities that consist of the following steps:

1. conform authors' names using the format (first name initial, surname),
2. update authors' names: add missing accents, eg, ö, é, and ś,
3. delete duplicates,
4. delete unrelated papers.

The first activity is automatically performed using our own script. The script analyses the author field and adjust names and surnames considering the target format. We perform the second activity manually, because we did not find any process to make it automatic. The third activity is performed using JabRef tool.<sup>‡</sup> The tool has a function to find duplicates, after a duplicate is identified the user can choose how to handle it. The possible solutions

<sup>‡</sup><http://www.jabref.org/>.



**FIGURE 2** RQ1: trend of publications

are keep one of them, keep both, or keep the merged entry only. The last activity, deleting unrelated papers and keeping only those of interest, is the most time-consuming because it requires involvement of the one who is performing the SLR. As this may introduce some bias, for this reason, we have precisely defined the following main inclusion/exclusion criteria:

1. **Formal methods:** The main focus is on formal methods or formal techniques like modeling, verification, and so on. The activity must include the use of a formal (abstract) notation and present, or at least enable, some form of rigorous analysis. For this reason, papers presenting semiformal approaches are discarded. We classify semiformal notations, those that do not have precise (mathematical/logical) semantics, eg, UML. Also papers that apply other methodologies (like agile or test-driven development) to medical software are discarded. Papers using verification or model checking directly applied to code are not considered because we require a part of modeling in the process.
2. **Medical software:** To be included, a paper must focus primarily on medical software or systems. Each paper must explicitly deal with or pay particular attention to a concrete medical application, software, system, or device. If the paper does not include examples specific to medical systems, it is discarded.

We analyze all the papers by reading their abstracts and overviewing their content in ambiguous cases. We delete all papers that do not describe the application of formal methods to a medical device/software. Moreover, we remove all documents that are not included in proceedings of peer-reviewed conferences/workshops/journals to maintain the number of documents manageable and the quality of the collection high. The result of preprocessing activity is the `Final.bib` file. Starting from this file, we perform 2 types of analysis: quantitative analysis and qualitative analysis.

Several analyses we perform in the following take as input the number of citations of papers. Several repositories provide citation data (with different degree of completeness and accuracy), and it is difficult to merge such data coming from different sources. Moreover, repositories like Google Scholar may be easily manipulated,<sup>12</sup> fail to correctly identify authors, include “gray” publications, or include duplicate citations.<sup>13</sup> For these reasons, we decided to use only citations given by Scopus, which offers a very good compromise between completeness and reliability.<sup>13</sup> Citations in Scopus are subject to change over time since they are constantly updated by Scopus. In this paper, we consider the citations retrieved on July 15, 2017.

## 4.1 | Quantitative analysis

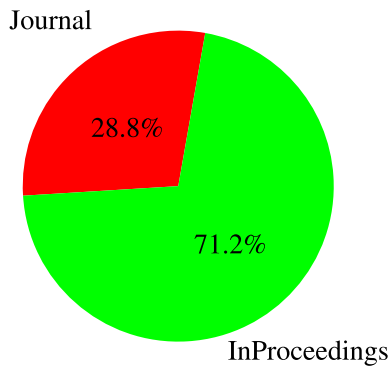
Quantitative analysis has a low degree of human interaction, and we performed it by using own scripts written in Extensible Stylesheet Language Transformation (.xslt). For this analysis, we consider the number of publications written over the years, the type of publications, the number of papers written by authors, and the number of citations. We answer the set of research questions as shown below.

**RQ1: Which is the trend of publications?** As a first question, we want to observe the trend of publications about formal methods applied in the medical field. We analyze the number of publications from 1992 (the year of the oldest publication we found) until 2016. As shown in Figure 2, until 2004, only 5 publications have been published. Starting from 2004, the interest on application of formal methods to medical devices increases. From 2010, the behavior of the number of papers shows a progressive increase until 2016.<sup>5</sup> The overall behavior of the graph shows an increasing interest in this topic by the community mostly in the last years.

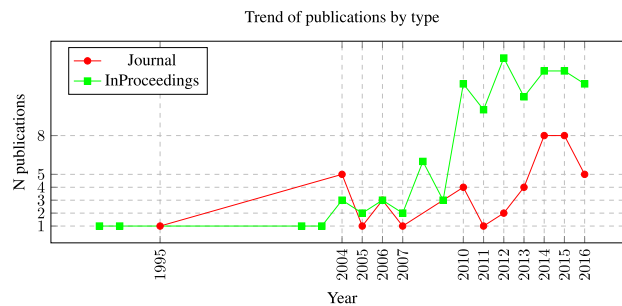
**RQ2: Which is the trend of publications considering the type?** In Figure 3, the pie chart shows the percentage of publications grouped by type. Note that from the databases, we obtain only journals and conference papers (InProceedings). The number of publications in proceedings (~71%) is greater than the number of publications in journals (~29%).

Figure 4 depicts the trend of the number of publications in journals and in proceedings. In the last few years, we notice an increase in number of publications in conferences. This trend can be affected by different factors: (1) The subject is still rather novel, and there is an increasing interest of the computer science community towards this topic; (2) usually, it is easier to publish in conferences than in journals; and (3) the publication in

<sup>5</sup>The search is performed in July 2017, we did not consider the 2017 in the graphs because the year is not finished yet.



**FIGURE 3** RQ2: types of publications



**FIGURE 4** Publications in journal/proceedings per year



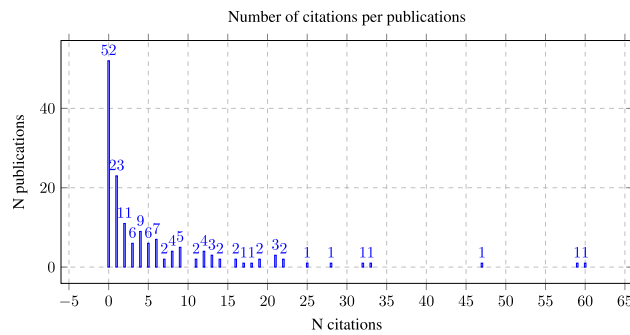
**FIGURE 5** RQ3: number of papers by the same author

conference is preferred because it provides the opportunity to expose the research to a wider audience and to have an immediate feedback by the experts in the field.

**RQ3: How many papers about this topic have been written by the same author?** Figure 5 shows the number of publications per author. The most apparent observation is that most authors (~69%) have published only once about this topic, 18.5% of authors have 2 publications, and 5.7% of authors have 3 publications. Only 6.8% of authors have more than 3 publications. An explanation could be that this topic is rather new in the scientific community and authors are starting their activities in these years. We expect an increase in number of publications per author in upcoming years due to ongoing scientific studies.

**RQ4: Which are the most cited publications?** Before introducing which are the most cited papers, we analyzed the general behavior of the number of citations (see Figure 6). Overall, approximately 33.7% of publications do not have citations. Approximately 47.4% of publications have less than ten citations, and approximately 18.9% of publications have more than 10 citations. The low number of citations could be due to the interest in novel verification methods rather than application of existing methods to specific case studies. Moreover, Scopus could introduce a delay in the collection of the citations.

Table 2 shows the most cited publications by considering only the citations given by Scopus. The publication with most citations<sup>14</sup> presents the utilization of formal methods in the improvement of medical protocols. A new formal language and theorem prover have been defined to help medical experts in medical protocol definition. In the second paper,<sup>15</sup> the authors present a framework for formal verification of a real-time extension of UML statecharts and present its application to the pacemaker example. The third paper<sup>16</sup> describes a closed-loop testing environment that, given the set of requirements of the pacemaker, produces a set of test cases. The fourth paper<sup>17</sup> highlights the importance of formal methods used in



**FIGURE 6** RQ4: number of citations/publication

**TABLE 2** Publications with most citations

N	Publications	No. of Citations
1	Ten Teije A, Marcos M, Balsler M, Van Croonenborg J, Duelli C, Van Harmelen F, Lucas P, Miksch S, Reif W, Rosenbrand K, et al. Improving medical protocols by formal methods. <i>Artificial Intelligence in Medicine</i> 2006; 36(3):193–209, doi: 10.1016/j.artmed.2005.10.006	60
2	David A, Oliver Möller M, Yi W. Formal verification of UML statecharts with realtime extensions. <i>Fundamental Approaches to Software Engineering, Lecture Notes in Computer Science</i> , vol. 2306, Springer Berlin Heidelberg, 2002; 218–232, doi: 10.1007/3-540-45923-5_15	59
3	Jiang Z, Pajic M, Mangharam R. Cyber-physical modeling of implantable cardiac medical devices. <i>Proceedings of the IEEE</i> 2012; 100(1):122–137, doi: 10.1109/JPROC.2011.2161241	47
4	Jetley R, Iyer S, Jones P. A formal methods approach to medical device review. <i>Computer</i> 2006; 39(4):61–67, doi: 10.1109/MC.2006.113	33
5	Jiang Z, Pajic M, Connolly A, Dixit S, Mangharam R. Real-time heart model for implantable cardiac device validation and verification. <i>Proceedings - Euromicro Conference on Real-Time Systems</i> , 2010; 239–248, doi: 10.1109/ECRTS.2010.36	32
6	Pajic M, Jiang Z, Lee I, Sokolsky O, Mangharam R. From verification to implementation: A model translation tool and a pacemaker case study. <i>Real-Time Technology and Applications - Proceedings</i> , 2012; 173–184, doi: 10.1109/RTAS.2012.25	28
7	Arney D, Jetley R, Jones P, Lee I, Sokolsky O. Formal methods based development of a PCA infusion pump reference model: Generic infusion pump (GIP) project. <i>High Confidence Medical Devices, Software, and Systems and Medical Device Plug-and-Play Interoperability</i> , Cambridge, MA, 2007; 23–33, doi: 10.1109/HCMDSS-MDPnP.2007.36	25
8	Alur R, Arney D, Gunter E, Lee I, Lee J, Nam W, Pearce F, Van Albert S, Zhou J. Formal specifications and analysis of the computer-assisted resuscitation algorithm (CARA) Infusion Pump Control System. <i>International Journal on Software Tools for Technology Transfer</i> 2004; 5(4):308–319, doi: 10.1007/s10009-003-0132-7	22
9	Jee E, Wang S, Kim J, Lee J, Sokolsky O, Lee I. A safety-assured development approach for real-time software. <i>Proceedings - 16th IEEE International Conference on Embedded and Real-Time Computing Systems and Applications</i> , RTCSA 2010, 2010; 133–142, doi: 10.1109/RTCSA.2010.42	22

premarket and postmarket analysis for medical devices. The fifth paper<sup>18</sup> shows how to derive the timed automata model of the heart. In the sixth paper,<sup>19</sup> the tool UPP2SF is presented. The tool translates UPPAAL models into Simulink/StateFlow models to take advantage of the automatic code generator available in Simulink. Again, the case study is the pacemaker. The seventh paper<sup>20</sup> applies formal methods to infusion pumps. The authors model the system using extended finite state machines (EFSMs) and apply validation and verification techniques using the UPPAAL framework. Furthermore, they generate test cases from the formal specification of the system to test the machine code. Also, the eighth paper<sup>21</sup> models the infusion pump using EFSM and applies verification technique using the Software Cost Reduction tool. In the ninth paper,<sup>22</sup> measurement-based

timing analysis is used to guarantee timing properties in implementation as well as in the formal model. When timing properties may be violated in the implementation due to timing delay, it is suggested to measure the time deviation and reflect it to the code explicitly by modifying guards. The case study is the pacemaker.

## 4.2 | Qualitative analysis

Qualitative analysis has the main goal of identifying the topics of interest and for which activities formal methods are more often used. It cannot be performed by automatic scripts like quantitative analysis. The publications were manually analyzed to extract the following information:

- the notations used (eg, automata, state charts, and abstract state machines);
- the case studies analyzed (eg, pacemaker and infusion pump);
- the target of the application (eg, model verification, model validation, and certification);
- the methodologies applied (eg, modeling, refinement, verification, and conformance checking).
- the tools used (eg, MATLAB, SPIN, Asmeta, and Rodin);

**RQ5: Which are the notations used?** In Table 3, the notations used in resulted papers are classified into 5 macro categories:

- Logic: The notation is based on a logical language that consists of logical symbols and is characterized by having a fixed interpretation. The combination of these symbols comprise well-formed formulas.
- State Based: In a state-based approach, an execution of a system is viewed as a sequence of states, where a state is an assignment of values to some set of components.<sup>23</sup>
- Event Based: An event-based approach views an execution as a sequence of events.<sup>23</sup>

The most used notations are Automata, Event-B, Z, and EFSM. All of them are state-based notations. One of the possible reasons why state-based notations are popular in medical software systems is because they support a model-driven development paradigm where requirements are transformed into functional code through a systematic process. In this fashion, it is easier to manage complexity, it is easier to reason about the behavior of the system, and efforts spent in earlier phases of the development ultimately result in generation of code that is correct by construction.

**RQ6: Which are the case studies analyzed and which activities are performed?** Table 4 shows which are the methods applied for each case study analyzed. Starting from the second column, we have identified a set of steps applied during the software development process. The first activity performed is modeling. Depending on the tool used by the user, a system is modeled using different notations (see RQ5). After that, a set of activities can be performed on the model. Model verification verifies whether the model satisfies given properties of interest. Model simulation is used to perform different activities, eg, to check the behavior of the system and to demonstrate the expected results. Software validation analyses the behavior of software as compared with the model. Code generation derives software directly from the model previously defined using a tool. The certification activity aims at identifying a connection between the process applied using formal methods and the standards/guidelines that guide the medical software approval. The last column of Table 4 collects papers that provide a theoretical study concerning medical devices specified in the first column.

The first column of Table 4 shows the medical devices or systems which formal methods are applied to. Some case studies were proposed by research groups. Recently, at the ABZ 2016 conference,<sup>159</sup> the hemodialysis machine case study has been provided to advocate the use of formal methods in medical applications.<sup>160</sup> Pacemaker requirements are provided by Software Quality Research Laboratory to the formal methods community to address the needs of industrial and government sectors that rely on the production of software that is critical for their missions and/or for

**TABLE 3** Notations used in the literature

Notation Type	Languages
Logic	Higher-Order Logic, Linear Temporal Logic (LTL), Computational Tree Logic (CTL), Temporal Ordering of Events, Timed Computational Tree Logic (TCTL)
State Based	Automata, B, Extended Finite State Machines (EFSM), Abstract State Machine (ASM), Z, Circus, State Machine, Event-B, Vienna Development Method (VDM), UML activity diagram, UML state machines, Algebraic State-Transition Diagrams (ASTD), Visual Contract Language (VCL), Mixed Signal Assertion Language (MSAL)
Event Based	Predicate/Transition Nets, Petri Nets, Activity Newtorks, Timed Transition System (TTS)



**TABLE 4** Application of formal methods to medical devices

Medical Device	Main Activity						
	Modeling	Model Verification	Model Validation	Software Validation	Code Generation	Certification	Survey
Hemodialysis machine	24-33	24,25,27,29,32,33	25,30-32		32	25	
Pacemaker	16,19,22,34-61	15,16,18,19,22,36,38-42,44,46,48-52,54-57,59,61-65,65-67	16,38,47,58,59,66,68,69	22,47,56,59,65	18,34,43,44,47,56,66,70		
Infusion pump	20,21,71-100,101	20,21,71,73-82,84,86,87,90,91,95-97,101-104	71-73,78,83,88,92,103,105	20,86	84,105	79,91	17
Medical image processing	106-109	106-109					110
Stereoacuity test	111	111	111	111			
ECG (electrocardiography)	112-121	115,119,122	112,114,117				
e-Health system	123-128	123,125,127,129,130	123,131			132,133	
Medical protocol	14,134	14,134					135
Pulse oximeter	136	136,137					
Medical device connection	138-144	138-149	140-142,145,149				
Imatinib dose	150,151	150,151					
Left ventricular assist device	152	152	152				
Clinical Neutron Therapy System	153						
Syringe pump	154,155	155	68,154				
Blood separator machine	156	156			156		
Medical interface	157	157	157				
Endotracheal intubation	158	158					

the safety and effectiveness of their products.<sup>¶</sup> The infusion pump case study has been provided by FDA.<sup>161#</sup> It invites the formal methods community to provide techniques and tools that improve the overall reliability of medical devices. The remaining case studies proposed by researchers are derived from their own experiences.

Regarding the activity applied to the case studies, we can draw the following observations. The hemodialysis machine case study is modeled by literature.<sup>24-33</sup> Some of them perform validation<sup>25,30-32</sup> and verification.<sup>24,25,27-29,32,33</sup> Mashkooor and Biro<sup>32</sup> generate the machine code starting from formal specification, and Arcaini et al<sup>25</sup> define a set of characteristics to fit formal methods with the standards for medical software development process. A model of pacemaker is described in papers.<sup>16,19,22,34-61</sup> Other authors apply model verification<sup>15,16,18,19,22,36,38-42,44,46,48-52,54-57,59,61-65,65-67</sup> and model validation.<sup>16,38,47,58,59,66,68,69</sup> The pacemaker software is validated in papers,<sup>22,47,56,59,65</sup> while previous studies<sup>18,34,43,44,47,56,66,70</sup> contribute to develop a new step that consists in translating the model into machine code. The infusion pump case study is modeled,<sup>20,21,71-100</sup><sup>101</sup> verified,<sup>20,21,71,73-82,84,86,87,90,91,95-97,101-104</sup> and validated<sup>71-73,78,83,88,92,103,105</sup> by using different tools and languages. Masci et al<sup>84</sup> and Mauro et al<sup>105</sup> present an approach for generating the machine code starting from the formal model, and in other studies,<sup>20,86</sup> authors use different approaches to validate software. Curzon et al and Liu et al<sup>79,91</sup> develop a method to support the approval process. Jetley et al<sup>17</sup> explain how to apply formal methods to premarket and postmarket evaluations in case of medical devices (infusion pump). Formal methods are also used in medical image processing for modeling and model verification.<sup>106-109</sup> Neufeld and Kuster<sup>110</sup> provide a survey about formal methods applied to image processing. The paper<sup>111</sup> shows a process that includes modeling, model simulation, model verification, model validation, and software validation by comparing the code with the formal requirements model applied to a medical screening test. Electrocardiography is the process of recording the electrical activity of the heart. The system is modeled,<sup>112-121</sup> verified,<sup>115,119,122</sup> and validated<sup>112,114,117</sup> using different tools. E-health systems are a recent classification of health care systems supported by electronic processes and communication. Papers<sup>123-128</sup> model the system, while it is verified in previous studies<sup>123,125,127,129,130</sup> and validated in Tahir et al<sup>123</sup> and Abdmeziem et al.<sup>131</sup> Furthermore, the certification criteria followed by Electronic Medical Records EMR applications in category of patients' privacy protection are studied in Kralj et al.<sup>132,133</sup> Suggestions on how to use formal methods are given also in the medical protocol case study.<sup>135</sup> Ten Teije et al<sup>14</sup> and Groot et al<sup>134</sup> propose a model of medical protocol and verify whether the overall process is correct or not. Pulse oximeter is modeled in Carneiro et al<sup>136</sup> and verified in Carneiro et al<sup>136</sup> and Cordeiro et al.<sup>137</sup> models<sup>138-144</sup> of medical device connections are verified<sup>138-149</sup> and validated.<sup>140-142,145,149</sup> Modelling and verification techniques are applied to imatinib dose in Simalatsar et al.<sup>150,151</sup> Model validation, model verification, and modeling activities are performed for left ventricular assist device.<sup>152</sup> A formal model is defined for clinical neutron therapy system,<sup>153</sup> and for syringe pump,<sup>154</sup> furthermore syringe pumps are validated in Sun and Meseguer<sup>68</sup> and Bowen and Reeves.<sup>154</sup> Code for blood separator machine is automatically derived in Tolvanen et al,<sup>156</sup> starting from the formal model that has been previously verified. A technique to model, verify, and validate medical machine interface is presented in Berstel et al,<sup>157</sup> while Gholami and Boucheneb<sup>158</sup> model and verify the endotracheal intubation system.

Overall, the most common activities performed are modeling and model verification, followed by model validation. A trend towards code generation has also been observed in recent publications. Although activities like software validation show little traction, we also consider them crucial in the medical software and systems development.

Considering all case studies, the most analyzed ones are about infusion pumps and pacemakers. Also, hemodialysis machines have been studied in several articles. We can note that all these systems are proposed by research groups as benchmarks and they come with a (quite) complete description of requirements and a good documentation. Since the application of formal methods to medical systems is a relatively new phenomenon, the researchers appear to prefer to test their methods and tools in well-known case studies to compare the obtained results rather easily. Furthermore, we can add that companies may not always be inclined to provide or publish data and code to test new techniques.

**RQ7: Which are the tools used for each performed activity?** Table 5 shows which tools or tool families are used for each software development activity. Most tools operate on models written in their specific languages. After the modeling process, a number of activities are performed on the model. The validation step checks that relevant behaviours of the real systems are accurately captured by the model. Verification, on the other hand, analyses whether the model is consistent w.r.t. the behavior and expected properties are verifiable. There exist different verification techniques; those used in the papers found are as follows:

- **Model checking:** It is applied to finite-state systems. The properties are translated in formulas of a temporal logic (eg, Computational Tree Logic or Linear Temporal Logic), and efficient symbolic algorithms are used to verify that the model satisfies specified properties of the system. If the property is false, a counterexample is displayed. The limitation of this technique is the state space explosion: The transition graph grows exponentially which can make model checking too inefficient for the analysis of complex models.
- **Satisfiability modulo theories solvers:** They are given an expression with boolean variables along with and/or predicates, based on which they determine the conditions that would make the expression true.
- **Theorem provers:** They are based on deduction methods (rather than state space exploration as in model checking), and they may not be fully automatic; they may require user intervention to complete the proof or demonstrate the presence of a design anomaly. The lack of full automation, however, is balanced by expressive specification languages and better handling of complex models as compared to model checking.

<sup>¶</sup><http://sqr1.mcmaster.ca/pacemaker.htm>.

<sup>#</sup> <http://www.fda.gov/MedicalDevices/ProductsandMedicalProcedures/GeneralHospitalDevicesandSupplies/InfusionPumps/>.

**TABLE 5** Tools used for each methodology

	Modeling			Verification			Software Code Generation	
	Modeling	Model Validation	Model Checking	SMT	Theorem Prover	Other Not Specified		Validation
MATLAB and Simulink	19,41,71,74,78,79,83,86,91,112-114	18,71,78,83,112,114	74,78,86	74		18,41,65,71,74,79,91,158	65,86	19
SPIN	53,78,106		52,78,106,157					
UPPAAL	20,40,42,44,47,56,63,78,86,107-109,125,150	47,78	15,19,20,40,42,44,47,56,78,86,107-109,125,150	40			20,86	44
SCR	21,52,71	71	21					
ASMETA	25,111	25,111	25,111				111	
Z tools	37,77,120,124,143,153		77,143					43
SAL	76,81,119,152	152	76,119	81,152				
B tools	26-28,30-32,34,38,39,46,73,85,93,95,115,118,154	30-32,38,73,103,154	27,32,38		32	28,39,46,73,95,103,115,117,122		32,34,70
PVS	72,75,79,80,84,155	72,105			75,84	64,79,80,155		84,105
VDM	123	123				123		
ProVerif	138					138		
Perfect Developer	43							
RealTime Maude	60,68,139	68	139					
NuSMV			137					
CBMC			137			62		
SATABS			137					
CEGAR	42,55		42,55					
VCB	35							
Asbru	134							
KIV					14	134		
ABV	24					24		
Yices	152		152	152				
Z3	40		40	40				
BLESS	36,54					36,54		
OSCP	144					144		
IVY workbench	82,87		82			87		
Circus	29		29					
CellExcite	116							
LOTOS tools	140	140				140		
V2T	141,142	141,142				141,142		
MathSAT 5				146				
PRISM			129,147,148					
MetaEdit+	156					156		156
SystemJ	49					49		
CPS-MAS	101					101		
StateRover	96	96				96		
TextBT	92							
SimTree		92						
TIMES	151		151					

Abbreviation: SMT, satisfiability modulo theories.

Software validation returns differences between the behavior captured by the real system and the requirements model defined by the developer. Code generation automatically produces the code for the real system, while test case generation derives test cases for the real system.

Regarding the types of activities, Table 5 hints that formal approaches are primarily used for modeling purposes. Also verification and, in particular, model checking play a predominant role in this area. The main advantage of model checking is that it is fully automated, so it is the preferred mean of verification. Activities like software validation (eg, testing) and code generation are surprisingly not common areas for the application of formal methods in medical software systems.

Regarding the tools used, we can see that most approaches use a rather small set of tools including B tools, MATLAB and Simulink, and UPPAAL. These tools have a good support and a commercial backing. Although tools like Mathworks' MATLAB and Simulink are strictly commercial, other tools like B tools and UPPAAL allow and encourage noncommercial uses as well. Other tools are used only in few case studies.

## 5 | LIMITATIONS

Despite the efforts made to collect the papers and to perform a complete and objective analysis, the SLR process presented in this paper has some limitations as listed below.

- Choice of the keywords: The keywords used for this work have been chosen based on the experience of researchers involved with this SLR. During the process, some relevant keywords could be missed as some publications authors or publishers may have used different keywords. Moreover, we perform the searches in Scopus only in the “author keywords” field because Scopus automatically adds many keywords that are often irrelevant or misleading.
- Choice of the databases: We have chosen Scopus, Web of Science, DBLP, and Google Scholar. The use of multiple sources contributes towards the completeness of search results. However, despite our utmost efforts, it may still be possible that some relevant papers remain unnoticed, for example, a technical report that is never published in a conference.
- Use of Scopus for citations: We have chosen Scopus for the number of citations because of its reliability. However, this may introduce a delay in the count of the number of citations since Scopus takes a while to update citation information, and this may underestimate the impact of some papers.

## 6 | CONCLUSION AND FUTURE WORK

In this paper, we have presented an SLR about the use of formal methods in modeling, design, analysis, and development of medical software and systems. To collect relevant papers, we have run several complex queries on a variety of databases (see Section 3). We performed a mixture of quantitative and qualitative analyses (see Section 4) to provide information that helps researchers who are either already working within this domain or planning to start. We have observed that the number of publications per year is showing an upward trend and researchers prefer to publish more in conferences than journals. Most authors have published only once in this field, and only a handful of authors have published more than 2 papers. It may be because researchers are interested in testing their methods and tools to different domains rather than just medical systems. While analyzing the most cited papers (see RQ4), we found that the authors are interested in the application of formal methods to real case studies, which work as preferred benchmarks for methodologies and techniques. This is highlighted also in Table 4. Regarding the activities performed by rigorous methodologies, we have found that most of the work revolves around modeling, validation, and verification mainly due to the availability of tools for these activities (as shown in Table 5). We also found that new trends, eg, automatic code generation and software validation, are also emerging that promise a tighter integration of formal methods with the overall development process. Principally, we have found that the use of formal and rigorous methods for medical software systems development interests very much the computer science community.

To minimize the bias in our systematic review, we have adopted several strategies. We have performed the queries on multiple bibliographic repositories. Although we have used a set of previously known papers, it only determines the completeness of our search and the analysis has been performed on the whole resulting set. We have identified the terms and keywords to be used in the queries starting from generic terms (like “medical software”) refined to specific terms and case studies (like “syringe pump”). To be systematic and to avoid the inclusion of too many irrelevant papers, we have included only papers that are captured by the queries and we have stated precise criteria for inclusion.

Despite our utmost care, we may still miss some relevant papers in case the authors use specific aspect of a device as keywords, eg, user interface, control logic, or the type of considered properties, eg, usability, performance, and security. To avoid any such incident, the data presented in Tables 4 and 5 can be further detailed by specifying various aspects of the devices that have been modeled and analyzed and the considered properties.

During our research, we did not find any prevalent tool or formal notation that can be considered as *standard*. Although the use of formal methods is gaining attention and is being recommended by regulatory authorities, we did not find any evidence to estimate how often formal techniques are used for modeling and analysis of medical devices by manufacturers. Ideally, we would like to have devices which are fully formally proven for their dependability and correctness, but we are far from this goal. Two reasons may be accountable for this situation. First, the current nature of medical software development mostly builds on code inspection, which is a less rigorous approach as compared to formal methods.<sup>17</sup> Second, the use of

formal methods for medical devices of high integrity level is only “recommended” by standards, eg, IEC 62304, and not enforced. By showing the usefulness and effectiveness of the application of formal methods, researchers can inspire device manufacturers to eventually adopt these methods as the standard medical software development technology.

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